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BIOMETRIKA

A JOURNAL FOR THE STATISTICAL STUDY OF BIOLOGICAL PROBLEMS

FOUNDED BY

W. F. R. WELDON, FRANCIS GALTON AND KARL PEARSON

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VOLUME XXI

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With this volume—the twenty-first—*Biometrika* reaches its majority, but it is the twenty-ninth year of its life. A history of its inception and early struggles by the Editor of this Journal will be found in the forthcoming third volume of *The Life, Letters, and Labours of Francis Galton.*

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